

# Evidence for single top quark production at the Tevatron

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*on behalf of the CDF and DØ collaborations*

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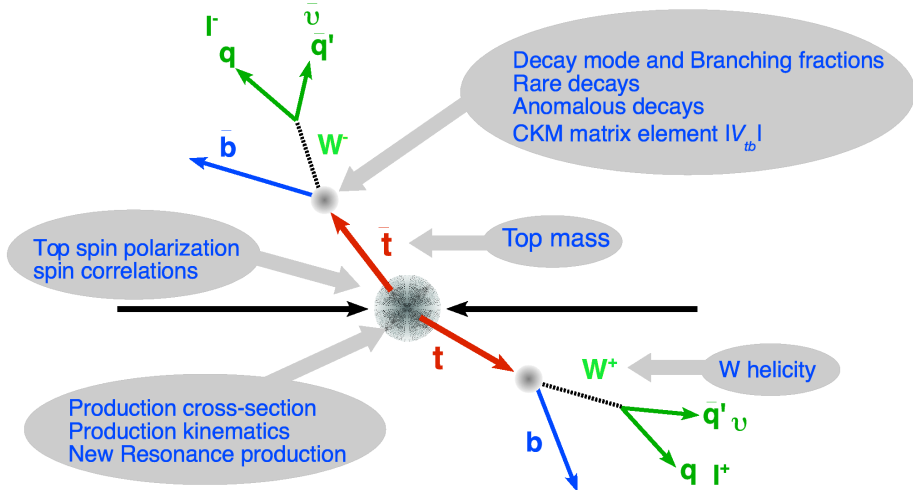


- 1 Single top production
- 2 Preparing for the measurement
  - Event selection
  - Backgrounds
  - $b$  tagging
- 3 Multivariate analysis techniques
- 4 Expected sensitivity
- 5 Cross sections and significance
- 6 First direct measurement of  $|V_{tb}|$
- 7 Conclusions



# Top quark physics

- The Tevatron is still the only place to make top quarks.



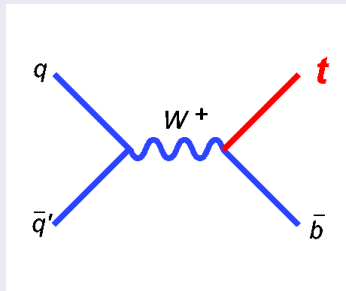
- Other predicted production mode: **single top**



# Single top quark production

- Electroweak production in two main mechanisms at the Tevatron:

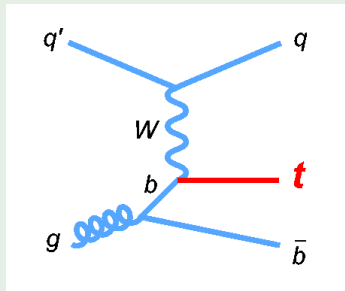
## s-channel (tb)



- $\sigma_{NLO} = 0.88 \pm 0.11 \text{ pb} (*)$
- previous limits (95% C.L.):

Run II DØ:  $< 5.0 \text{ pb} (370 \text{ pb}^{-1})$   
Run II CDF:  $< 3.1 \text{ pb} (700 \text{ pb}^{-1})$

## t-channel (tqb)



- $\sigma_{NLO} = 1.98 \pm 0.25 \text{ pb} (*)$
- previous limits (95% C.L.):

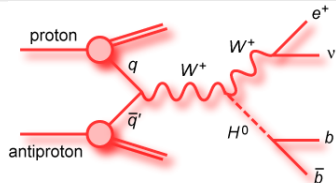
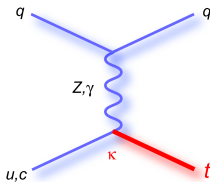
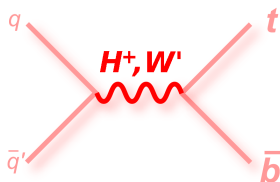
Run II DØ:  $< 4.4 \text{ pb} (370 \text{ pb}^{-1})$   
Run II CDF:  $< 3.2 \text{ pb} (700 \text{ pb}^{-1})$

(\*)  $m_t = 175 \text{ GeV}$ , Phys.Rev. D70 (2004) 114012







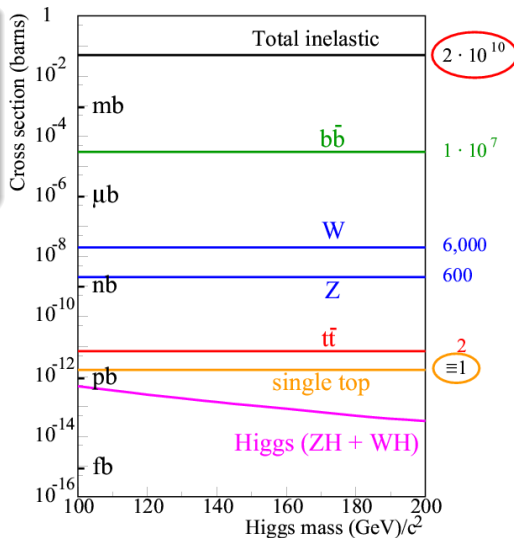
# Motivation

- Directly measure  $|V_{tb}|$  (more later)
- Cross sections sensitive to new physics:
  - s-channel: resonances (heavy  $W'$  boson, charged Higgs boson  $H^\pm$ , Kaluza-Klein excited  $W_{KK}$ , etc...)
  - t-channel: flavour-changing neutral currents ( $t - Z/\gamma/g - c$  couplings)
  - Fourth generation of quarks
- Source of polarized top quarks. Spin correlations measurable in decay products
- Important background to  $WH$  associated Higgs production
  - if the tools don't work for single top, forget about the Higgs
- Test of techniques to extract a small signal out of a large background

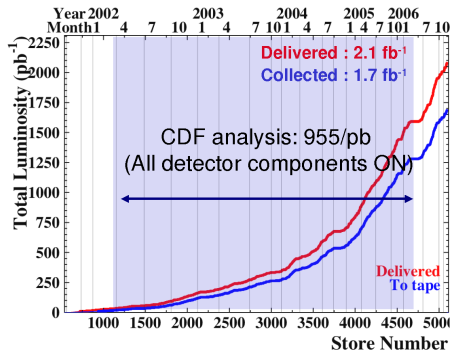


# It has been challenging for years...

- Several publications since Run I by  and 
- 7  and 6  PhDs
- $\sigma_{t\bar{t}}$  only  $\sim 2 \times \sigma_{\text{single top}}$ , but has striking signature

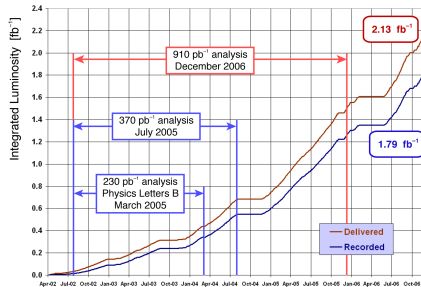


# Tevatron luminosity



## Run II Integrated Luminosity

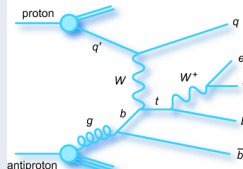
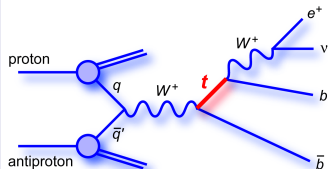
Apr 2002 – Dec 2006



Many thanks to the Accelerator Division





# Event selection



## Signature

- isolated lepton
- $\cancel{E}_T$
- jets
- at least 1 b-jet

		
1 lepton	$p_T^e > 20 \text{ GeV},  \eta_e  < 2$ $p_T^\mu > 20 \text{ GeV},  \eta_\mu  < 1.1$	$p_T^e > 15 \text{ GeV},  \eta_e  < 1.1$ $p_T^\mu > 18 \text{ GeV},  \eta_\mu  < 2.0$
jets	exactly 2 $p_T > 15 \text{ GeV},  \eta  < 2.8$	2,3,4 $p_T > 15 \text{ GeV},  \eta  < 3.4$ leading jet $p_T > 25 \text{ GeV},  \eta  < 2.5$ 2nd leading jet $p_T > 20 \text{ GeV}$
MET	$\cancel{E}_T > 25 \text{ GeV}$	$15 < \cancel{E}_T < 200 \text{ GeV}$
b jet	one or two	





# Event selection - S/B

Percentage of single top ***tb+tb*** selected events  
and S:B ratio (white squares = no plans to analyze)

Electron + Muon	1 jet	2 jets	3 jets	4 jets	≥ 5 jets
0 tags	10% 1 : 3,200	25% 1 : 390	12% 1 : 300	3% 1 : 270	1% 1 : 230
1 tag	6% 1 : 100	21% 1 : 20	11% 1 : 25	3% 1 : 40	1% 1 : 53
2 tags		3% 1 : 11	2% 1 : 15	1% 1 : 38	0% 1 : 43

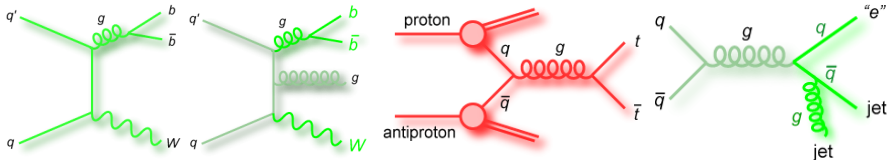


# Backgrounds

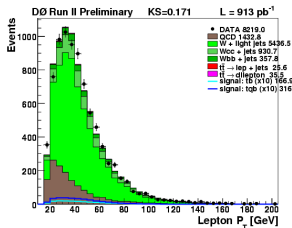
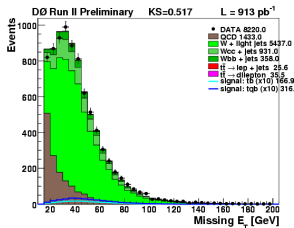
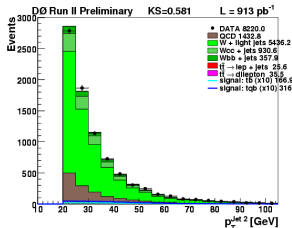
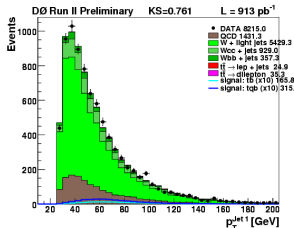
- Slightly different naming conventions and techniques between the two experiments but very similar in the end

## Main backgrounds

- $W$ +jets (Alpgen, normalized to data):
  - $W$ +heavy flavour:  $Wbb$ ,  $Wbj$ ,  $Wcc$ ,  $Wcj$ ,  $Wc$
  - $W$ +light jets (“mistags”)
- $t\bar{t}$  (Alpgen, Pythia,  $m_t = 175$  GeV,  $\sigma_{NNLO} = 6.8$  pb)
- QCD (a.k.a. multijet, non- $W$ ) (from data failing lepton ID)



# Event selection - Agreement before tagging



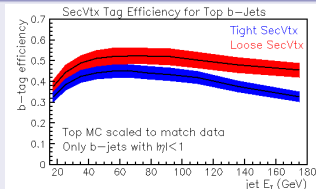
- Normalize W+multijet to data before tagging
- Checked 90 variables, 3 jet multiplicities, 1-2 tags, electron + muon
- Shown: electron, 2 jets, before tagging
- Good description of data



# CDF $b$ tagging

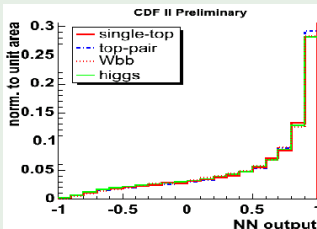
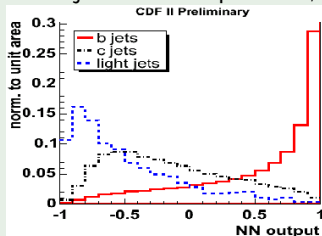
## Secondary vertex tagging

- Long lifetime of  $B$  hadrons
- Travel several mm before decaying
- Signature: displaced secondary vertex tagger
- Tagging efficiency per jet  $\sim 40\%$



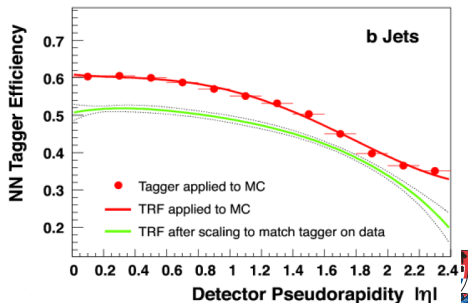
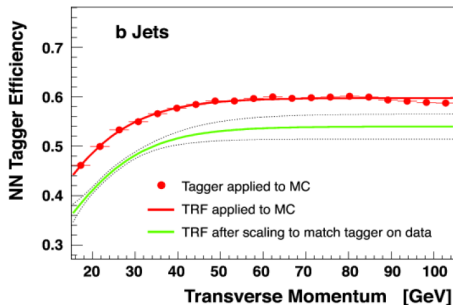
## Jet flavour separation

- Second stage: improve separation with 25-input neural network
- Applied on jets  $b$ -tagged with secondary vertex
- Good jet flavour separation, independent of  $b$ -jet source



# DØ $b$ tagging

- NN trained on 7 input variables from existing taggers.
- Much improved performance!
  - fake rate reduced by 1/3 for same  $b$  efficiency relative to previous tagger
  - smaller systematic uncertainties
- Tag Rate Functions (TRFs) in  $\eta$ ,  $p_T$ ,  $z$ -PV applied to MC
- Operating point:
  - $b$ -jet efficiency  $\sim 50\%$
  - $c$ -jet efficiency  $\sim 10\%$
  - light jet efficiency  $\sim 0.5\%$



# Systematic uncertainties - CDF

CDF RunII Preliminary,  $L=955\text{pb}^{-1}$

Single Top	Rate Variations	Shape Variations
Jet Energy Scale	✓	✓
Initial State Radiation	✓	✓
Final State Radiation	✓	✓
Parton Dist. Function	✓	✓
Monte Carlo Generator	✓	
Efficiencies / b-tagging SF	✓	
Luminosity	✓	
<b>Total Rate Uncertainty</b>	<b>10.5%</b>	<b>N/A</b>

Backgrounds	Rate Variations	Shape Variations
Jet Energy Scale	✓	✓
Neural Net b-tagger		✓
Mistag Model		✓
Non-W Model		✓
$Q^2$ Scale in Alpgen MC		✓

Background	Rate Uncertainty
W+bottom	28%
W+charm	28%
Mistag	15%
ttbar	23%

- Rate and shape uncertainties included as nuisance parameters in analyses



# Systematic uncertainties - $D\bar{0}$

- Assigned per background, jet multiplicity, lepton flavour and number of tags
- Uncertainties that affect both normalisation and shapes: jet energy scale and tag rate functions ( $b$ -tagging parameterisation)
- All uncertainties sampled during limit-setting phase

## Relative systematic uncertainties

$t\bar{t}$ cross section	18%	Primary vertex	3%
Luminosity	6%	$e$ reco * ID	2%
Electron trigger	3%	$e$ trackmatch & likelihood	5%
Muon trigger	6%	$\mu$ reco * ID	7%
Jet energy scale	wide range	$\mu$ trackmatch & isolation	2%
Jet efficiency	2%	$\varepsilon_{\text{real}-e}$	2%
Jet fragmentation	5–7%	$\varepsilon_{\text{real}-\mu}$	2%
Heavy flavor ratio	30%	$\varepsilon_{\text{fake}-e}$	3–40%
Tag-rate functions	2–16%	$\varepsilon_{\text{fake}-\mu}$	2–15%

# Event Selection - Yields



Source	Event Yields in 0.9 fb <sup>-1</sup> Data		
	Electron+muon, 1tag+2tags combined		
	2 jets	3 jets	4 jets
<i>tb</i>	16 ± 3	8 ± 2	2 ± 1
<i>tqb</i>	20 ± 4	12 ± 3	4 ± 1
<i>t<math>\bar{t}</math> → ll</i>	39 ± 9	32 ± 7	11 ± 3
<i>t<math>\bar{t}</math> → l+jets</i>	20 ± 5	103 ± 25	143 ± 33
<i>W+b<math>\bar{b}</math></i>	261 ± 55	120 ± 24	35 ± 7
<i>W+c<math>\bar{c}</math></i>	151 ± 31	85 ± 17	23 ± 5
<i>W+jj</i>	119 ± 25	43 ± 9	12 ± 2
Multijets	95 ± 19	77 ± 15	29 ± 6
Total background	686 ± 41	460 ± 39	253 ± 38
Data	697	455	246









s-channel	15.4 ± 2.2
t-channel	22.4 ± 3.6
<i>t<math>\bar{t}</math></i>	58.4 ± 13.5
Diboson	13.7 ± 1.9
Z + jets	11.9 ± 4.4
<i>Wbb</i>	170.9 ± 50.7
<i>Wcc</i>	63.5 ± 19.9
<i>Wc</i>	68.6 ± 19.0
Non-W	26.2 ± 15.9
Mistags	136.1 ± 19.7
Single top	37.8 ± 5.9
Total background	549.3 ± 95.2
Total prediction	587.1 ± 96.6
Observed	644

- Expected single top signal is smaller than background uncertainty!  
⇒ No counting experiment, requires advanced analysis techniques





# Multivariate analysis techniques

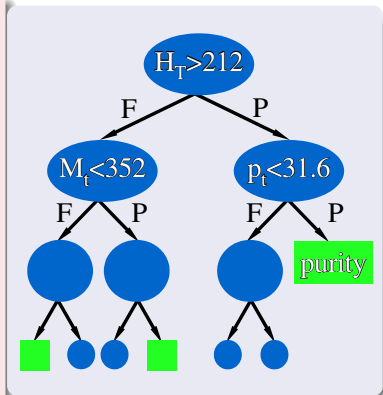
- Likelihood discriminants ()
- Artificial neural network ()
- Matrix element (, )
- Bayesian neural networks ()
- Boosted decision trees ()



# Decision trees

- Machine-learning technique, widely used in social sciences
- Idea: recover events that fail criteria in cut-based analysis

- Start with all events = first node
  - sort all events by each variable
  - for each variable, find splitting value with best separation between two children (mostly signal in one, mostly background in the other)
  - select variable and splitting value with best separation, produce two branches with corresponding events ((F)ailed and (P)assed cut)
- Repeat recursively on each node
- Splitting stops: terminal node = leaf



- Run testing events and data through tree to derive limits
- DT output = leaf purity, close to 1 (0) for signal (bkg)

Ref: Breiman *et al*, "Classification and Regression Trees", Wadsworth (1984)



# Boosting a decision tree

## Boosting

- Recent technique to improve performance of a weak classifier
- Recently used on decision trees by GLAST and MiniBooNE
- Basic principal on DT:
  - train a tree  $T_k$
  - $T_{k+1} = \text{modify}(T_k)$

## AdaBoost algorithm

- Adaptive boosting
- Check which events are misclassified by  $T_k$
- Derive tree weight  $\alpha_k$
- Increase weight of misclassified events
- Train again to build  $T_{k+1}$
- Boosted result of event  $i$ :  
$$T(i) = \sum_{n=1}^{N_{\text{tree}}} \alpha_k T_k(i)$$

- Averaging  $\Rightarrow$  dilutes piecewise nature of DT
- Usually improves performance

Ref: Freund and Schapire, "Experiments with a new boosting algorithm", in *Machine Learning: Proceedings of the Thirteenth International Conference*, pp 148-156 (1996)



# Decision trees at DØ

## DT choices

- 1/3 of MC for training
- AdaBoost parameter  $\beta = 0.2$
- 20 boosting cycles
- Signal leaf if purity  $> 0.5$
- Minimum leaf size = 100 events
- Same total weight to signal and background to start
- Goodness of split - Gini factor

## Input variables

- Used 49 variables (object and event kinematics, angular correlations)
- Adding variables does not degrade performance
- Tested shorter lists: lost some sensitivity
- Same list used for all channels

## Analysis strategy

- Train 36 separate trees:  $(s, t, s + t) \times (e, \mu) \times (2, 3, 4 \text{ jets}) \times (1, 2 \text{ tags})$
- For each signal train against the sum of backgrounds

# Matrix element method

- Pioneered by DØ top mass analysis. Now used in search
- Use the 4-vectors of all reconstructed leptons and jets
- Use matrix elements of main signal and background diagrams to compute an event probability density for signal and background hypotheses
- Encoded in properly normalized differential cross section for process  $S$ :

$$P_S(\vec{x}) = \frac{1}{\sigma_S} d\sigma_S(\vec{x}), \quad \sigma_S = \int d\sigma_S(\vec{x})$$

- Only a limited number of Feynman diagrams are used. Sensitivity would increase (but so does computation time) if more diagrams were included. In particular, no  $t\bar{t}$  diagrams are computed (serious limitation for  $>2$  jets)



# Matrix element discriminants

## DØ discriminants

$$D_s(\vec{x}) = P(S|\vec{x}) = \frac{P_{signal}(\vec{x})}{P_{signal}(\vec{x}) + P_{bkg}(\vec{x})}$$

$$P_{bkg}^{2jets}(\vec{x}) = c_{Wbb}P_{Wbb}(\vec{x}) + c_{Wcg}P_{Wcg}(\vec{x}) + c_{Wgg}P_{Wgg}(\vec{x})$$

$$P_{bkg}^{3jets}(\vec{x}) = P_{Wbbg}(\vec{x})$$

- $c_{Wbb}$ ,  $c_{Wcg}$  and  $c_{Wgg}$  are in principle the relative fractions of each background
- optimized for each channel to increase sensitivity

## CDF discriminant

$$EPD = \frac{b \cdot P_{signal}}{b \cdot P_{signal} + b \cdot P_{Wbb} + (1 - b)P_{Wcc} + (1 - b)P_{Wcj}}$$

- $b$  is the neural network  $b$ -tagger output converted to probability

# Likelihood method (CDF)

- Likelihood for a vector of measurements  $\vec{x} = x_i$ :

$$\mathcal{L}(\vec{x}) = \frac{\mathcal{P}_{\text{signal}}(\vec{x})}{\mathcal{P}_{\text{signal}}(\vec{x}) + \sum \mathcal{P}_{\text{background}}(\vec{x})}, \quad \mathcal{P}(\vec{x}) = \prod_i^{N_{\text{variables}}} P(x_i)$$

$P(x_i)$  = normalized  $x_i$  variable distribution

- Four backgrounds:  $Wbb$ ,  $t\bar{t}$ ,  $Wcc/Wc$ , mistags

## t-channel LF Variables:

- total transverse energy:  $H_T$
- $M_{\text{lvb}}$  (neutrino  $p_z$  from kin. fitter)
- $\text{Cos}\theta(\text{lepton, light jet})$  in top decay frame
- $Q_{\text{lepton}} * \eta_{\text{untagged jet}}$  aka  $Q_{\text{xEta}}$
- $m_{j1j2}$
- $\log(\text{ME}_{\text{tchan}})$  from MADGRAPH
- Neural Network b-tagger
- LF=0.01 for double tagged events

## s-channel LF Variables:

- $M_{\text{lvb}}$
- $\log(H_T * M_{\text{lvb}})$
- $E_T(\text{jet1})$
- $\log(\text{ME}_{\text{tchan}})$
- $H_T$
- Neural Network b-tagger



## Neural network (CDF)

- Three-layer perceptrons using NeuroBayes
- Continuous output between -1 (bkg-like) and +1 (signal-like)
- 26 input variables
- Three networks: tb, tqb and tb+tqb and signal

## Bayesian neural networks (DØ)

- Instead of choosing one set of weights, find posterior probability density over all possible weights
- Averaging over many networks weighted by the probability of each network given the training data
- Less prone to overtraining
- For details see:  
<http://www.cs.toronto.edu/~radford/fbm.software.html>
- Use 24 variables (subset of DT variables)



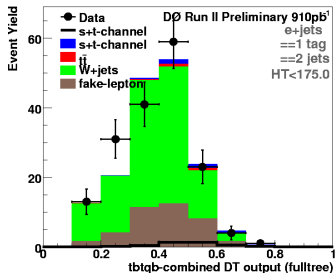
- To verify that all of this machinery is working properly we test with many sets of pseudo-data.
- Wonderful tool to test analysis methods! Run DØ experiment 1000s of times!
- Generated ensembles:
  - 0-signal ensemble ( $s + t \sigma = 0$  pb)
  - SM ensemble ( $s + t \sigma = 2.9$  pb)
  - “Mystery” ensembles to test analyzers ( $s + t \sigma = ??$  pb)
  - Ensembles at measured cross section ( $s + t \sigma = \text{measured}$ )
  - A high luminosity ensemble
- All analyses achieved linear response to varying input cross sections



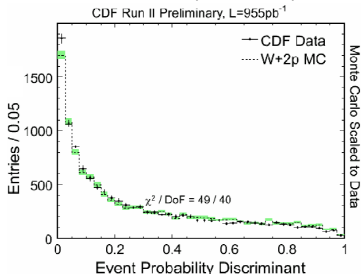
# Cross-check samples

- Validate methods using data without looking at signal
- Compare discriminant in model and data
- Good agreement observed

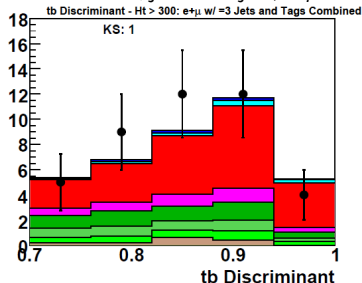
DT “W+jets”: =2jets,  $H_T < 175$  GeV



ME W+2jets data (b-jet veto)



ME “hard W+jets”: =3jets,  $H_T > 300$  GeV

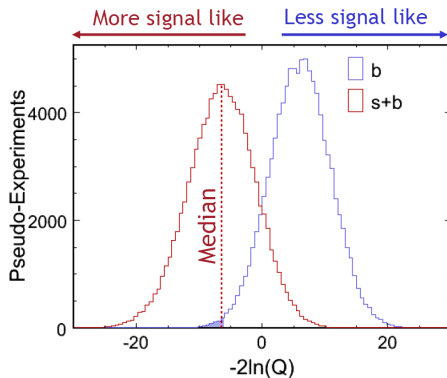


# Sensitivity determination at CDF

- Using the CLs method developed at LEP
- Compare two models at a time
- Test statistic:

$$Q = \frac{L(data|s + b)}{L(data|b)}$$

- Systematic uncertainties included in pseudo-experiments
- **Expected sensitivity:** median p-value



Likelihood	median p-value = 2.3%	(2.0 $\sigma$ )
Matrix element	median p-value = 0.6%	(2.5 $\sigma$ )
Neural network	median p-value = 0.5%	(2.6 $\sigma$ )



# Sensitivity determination at DØ

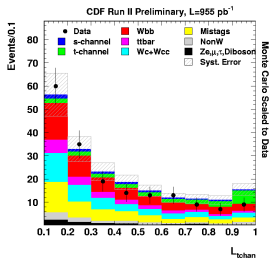
- Use the 0-signal ensemble:
  - use pool of weighted signal+bkg events
  - fluctuate relative and total yields in proportion to syst. errors
  - randomly sample from a Poisson distribution about total yield
  - generate a set of pseudo data
  - pass the pseudo-data through the full analysis
- **Expected p-value:** fraction of 0-signal pseudo-datasets in which we measure at least 2.9 pb (SM single top cross section)
- **Observed p-value:** fraction of 0-signal pseudo-datasets in which we measure at least the observed cross section.

Boosted decision trees	p-value = 1.9%	(2.1 $\sigma$ )
Matrix element	p-value = 3.7%	(1.8 $\sigma$ )
Bayesian neural networks	p-value = 9.7%	(1.3 $\sigma$ )



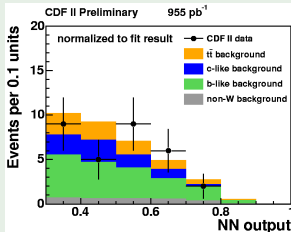
# CDF s+t observed results — Preliminary

## Likelihood



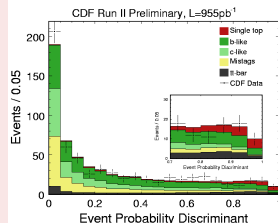
No evidence of signal  
 $\sigma < 2.7 \text{ pb @ 95\% CL}$   
 From s and t likelihoods

## Neural network



no evidence of signal  
 $\sigma < 2.6 \text{ pb @ 95\% CL}$

## Matrix element

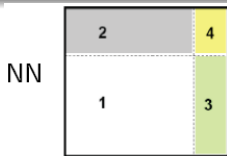
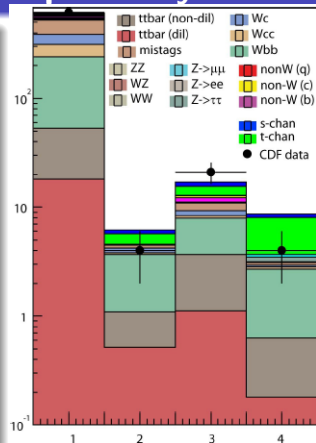


$\sigma = 2.7^{+1.5}_{-1.3} \text{ pb}$   
 $p\text{-value} = 1.0\% (2.3\sigma)$



# CDF observed results — Compatibility

- CDF spent great deal of time (6 months) and effort understanding if the different results are something more than a statistical fluctuation.
- Eliminated possibility of obvious and even subtle bugs
- 6-discriminant compatibility coming soon
- Now investigating if features of the MC modeling affect one analysis more than the other.
- Analysing more data should shed some light



ME

Bin 1:  $NN < 0.8 \ \&\& \ EPD < 0.9$

Bin 2:  $NN > 0.8 \ \&\& \ EPD < 0.9$

Bin 3:  $NN < 0.8 \ \&\& \ EPD > 0.9$

Bin 4:  $NN > 0.8 \ \&\& \ EPD > 0.9$



# DØ BNN and ME s+t observed results

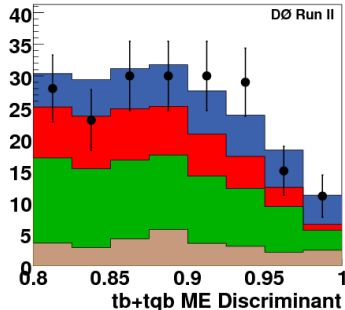
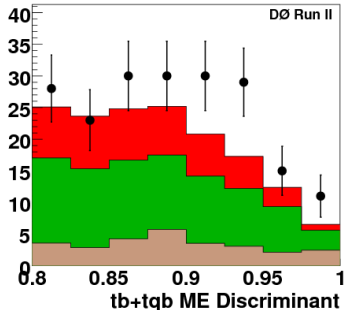
## Bayesian NN

$\sigma = 5.0 \pm 1.9 \text{ pb}$   
p-value = 0.89% ( $2.4\sigma$ )

## Matrix element

$\sigma = 4.6^{+1.8}_{-1.5} \text{ pb}$   
p-value = 0.21% ( $2.9\sigma$ )

- ME discriminant output, with and without signal content (all channels combined)

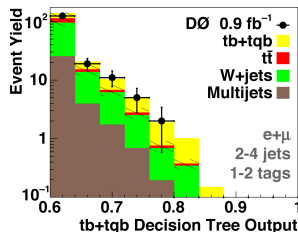
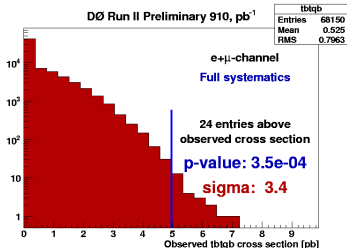
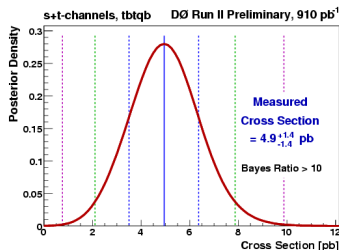
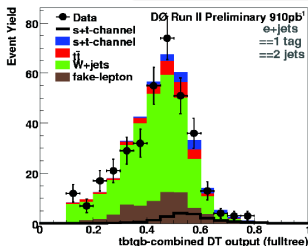


# DØ boosted decision tree s+t observed results

$$\sigma = 4.9 \pm 1.4 \text{ pb}$$

$$p\text{-value} = 0.035\% (3.4\sigma)$$

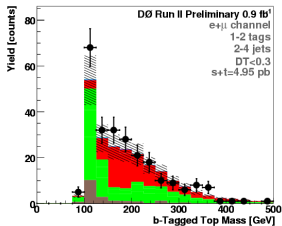
SM compatibility: 11% ( $1.1\sigma$ )



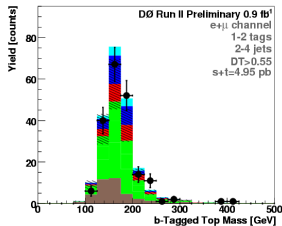


# DØ boosted decision tree event characteristics

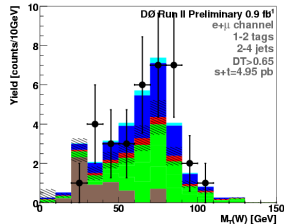
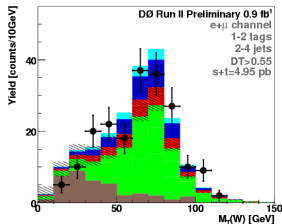
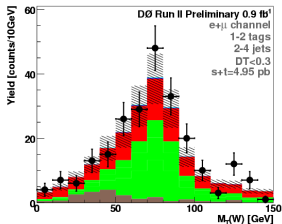
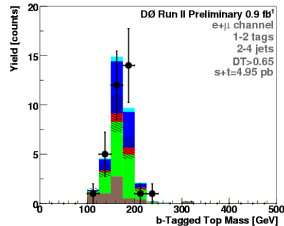
$DT < 0.3$



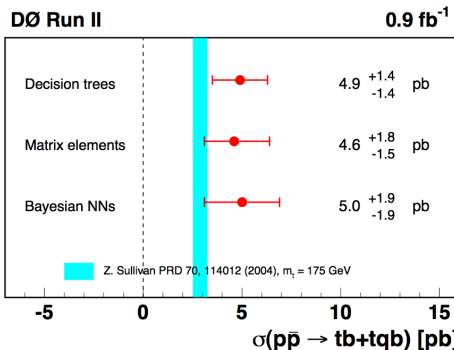
$DT > 0.55$



$DT > 0.65$



# DØ results consistency



## High discriminant correlation

Choose the 50 highest events in each discriminant and look for overlap

	Electron	Muon
DT vs ME	52%	58%
DT vs BNN	56%	48%
ME vs BNN	46%	52%

## Linear correlation

Measured cross section in 400 members of SM ensemble with all three techniques and calculated the linear correlation between each pair

	DT	ME	BNN
DT	100%	39%	57%
ME		100%	29%
BNN			100%

# First direct measurement of $|V_{tb}|$

## Direct access to $|V_{tb}|$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ \color{blue}{V_{td}} & \color{blue}{V_{ts}} & \color{red}{V_{tb}} \end{pmatrix}$$

- Weak interaction eigenstates are not mass eigenstates
- In SM: top must decay to a  $W$  and  $d$ ,  $s$  or  $b$  quark
  - $V_{td}^2 + V_{ts}^2 + V_{tb}^2 = 1$
  - constraints on  $V_{td}$  and  $V_{ts}$ :  $|V_{tb}| = 0.9991$
- New physics:
  - $V_{td}^2 + V_{ts}^2 + V_{tb}^2 < 1$
  - no constraint on  $V_{tb}$

## Result

- Translate  $tb+tbq$  cross section into measurement of the strength of  $V-A$  coupling  $|V_{tb}f_1^L|$  in  $Wtb$  vertex ( $f_1^L$ : arbitrary left-handed form factor)
- Assume  $V_{td}^2 + V_{ts}^2 \ll V_{tb}^2$  and pure  $V-A$  and CP-conserving  $Wtb$  interaction

$$|\mathbf{V}_{tb}f_1^L| = 1.3 \pm 0.2$$

- Also assuming  $f_1^L = 1$ :

$$0.68 < |\mathbf{V}_{tb}| \leq 1 \text{ @ 95\% CL}$$

- No assumption about number of quark families or CKM matrix unitarity

# Conclusions

- CDF and DØ have been searching for single top signal for years
- A lot of energy invested in the experimental challenges
  - very small signal hidden in enormous background
  - efficient  $b$ -tagging
  - background modeling (involving data and Monte Carlo)
- Several multivariate techniques being used
- CDF analyses have good sensitivity but got unlucky ( $2.3\sigma$  signal with ME, LF and NN don't see any single top)
- DØ BNN and ME analyses see  $2.4\sigma$  and  $2.9\sigma$  signal



# Conclusions

## First evidence for single top quark production (DØ decision trees)

$$\sigma(p\bar{p} \rightarrow tb + X, tqb + X) = 4.9 \pm 1.4 \text{ pb}$$

3.4 $\sigma$  significance

## First direct measurement of $|V_{tb}|$ (DØ decision trees)

$$|V_{tb}f_1^L| = 1.3 \pm 0.2$$

assuming  $f_1^L = 1$ :  $0.68 < |V_{tb}| \leq 1$  @ 95% CL

(Always assuming  $V_{td}^2 + V_{ts}^2 \ll V_{tb}^2$  and pure V–A and CP-conserving  $Wtb$  interaction)

hep-ex/0612052, submitted to PRL

- Working on understanding correlations and on combinations
- A lot more data already at hand



# Backup slides



# Splitting a node

## Impurity $i(t)$

- maximum for equal mix of signal and background
- symmetric in  $p_{\text{signal}}$  and  $p_{\text{background}}$
- minimal for node with either signal only or background only
- strictly concave  $\Rightarrow$  reward purer nodes

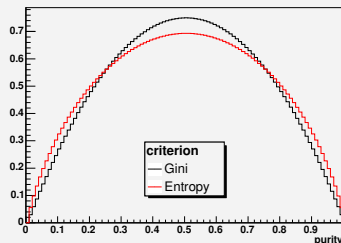
- Decrease of impurity for split  $s$  of node  $t$  into children  $t_L$  and  $t_R$  (goodness of split):  
$$\Delta i(s, t) = i(t) - p_L \cdot i(t_L) - p_R \cdot i(t_R)$$
- Aim: find split  $s^*$  such that:

$$\Delta i(s^*, t) = \max_{s \in \{\text{splits}\}} \Delta i(s, t)$$

- Maximizing  $\Delta i(s, t) \equiv$  minimizing overall tree impurity

## Examples

$$\text{Gini} = 1 - \sum_{i=s,b} p_i^2 = \frac{2sb}{(s+b)^2}$$
$$\text{entropy} = - \sum_{i=s,b} p_i \log p_i$$



# Decision Trees - 49 variables

## Object Kinematics

$p_T(\text{jet1})$   
 $p_T(\text{jet2})$   
 $p_T(\text{jet3})$   
 $p_T(\text{jet4})$   
 $p_T(\text{best1})$   
 $p_T(\text{notbest1})$   
 $p_T(\text{notbest2})$   
 $p_T(\text{tag1})$   
 $p_T(\text{untag1})$   
 $p_T(\text{untag2})$

## Angular Correlations

$\Delta R(\text{jet1}, \text{jet2})$   
 $\cos(\text{best1}, \text{lepton})_{\text{besttop}}$   
 $\cos(\text{best1}, \text{notbest1})_{\text{besttop}}$   
 $\cos(\text{tag1}, \text{alljets})_{\text{alljets}}$   
 $\cos(\text{tag1}, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{jet1}, \text{alljets})_{\text{alljets}}$   
 $\cos(\text{jet1}, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{jet2}, \text{alljets})_{\text{alljets}}$   
 $\cos(\text{jet2}, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$   
 $\cos(\text{lepton}, \text{besttopframe})_{\text{besttopCMframe}}$   
 $\cos(\text{lepton}, \text{btaggedtopframe})_{\text{btaggedtopCMframe}}$   
 $\cos(\text{notbest}, \text{alljets})_{\text{alljets}}$   
 $\cos(\text{notbest}, \text{lepton})_{\text{besttop}}$   
 $\cos(\text{untag1}, \text{alljets})_{\text{alljets}}$   
 $\cos(\text{untag1}, \text{lepton})_{\text{btaggedtop}}$

## Event Kinematics

Aplanarity(alljets,  $W$ )  
 $M(W, \text{best1})$  ("best" top mass)  
 $M(W, \text{tag1})$  (" $b$ -tagged" top mass)  
 $H_T(\text{alljets})$   
 $H_T(\text{alljets} - \text{best1})$   
 $H_T(\text{alljets} - \text{tag1})$   
 $H_T(\text{alljets}, W)$   
 $H_T(\text{jet1}, \text{jet2})$   
 $H_T(\text{jet1}, \text{jet2}, W)$   
 $M(\text{alljets})$   
 $M(\text{alljets} - \text{best1})$   
 $M(\text{alljets} - \text{tag1})$   
 $M(\text{jet1}, \text{jet2})$   
 $M(\text{jet1}, \text{jet2}, W)$   
 $M_T(\text{jet1}, \text{jet2})$   
 $M_T(W)$   
Missing  $E_T$   
 $p_T(\text{alljets} - \text{best1})$   
 $p_T(\text{alljets} - \text{tag1})$   
 $p_T(\text{jet1}, \text{jet2})$   
 $Q(\text{lepton}) \times \eta(\text{untag1})$   
 $\sqrt{\hat{s}}$   
Sphericity(alljets,  $W$ )

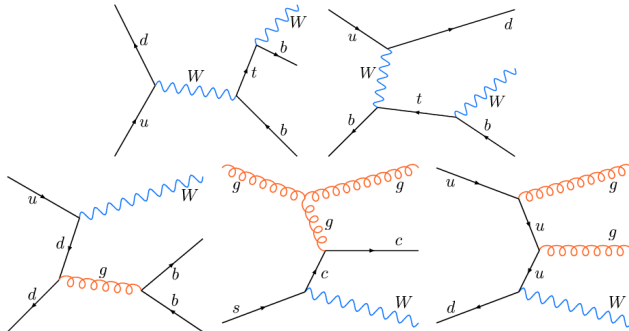
- Adding variables does not degrade performance
- Tested shorter lists, lose some sensitivity
- Same list used for all channels



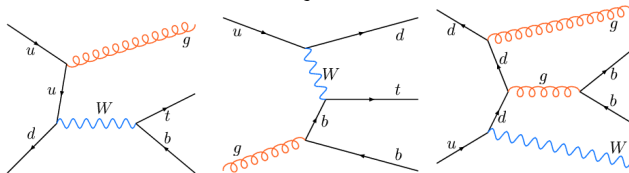


# Matrix element method - D0 diagrams

2-jets:

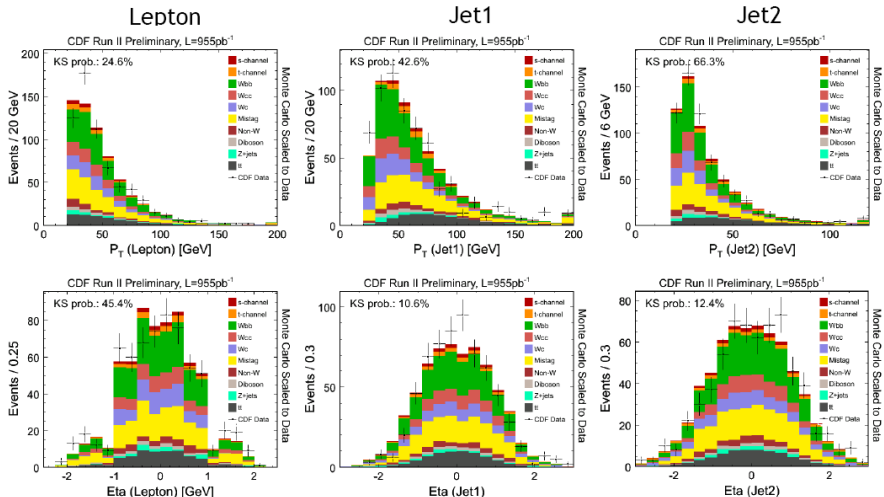


3-jets:

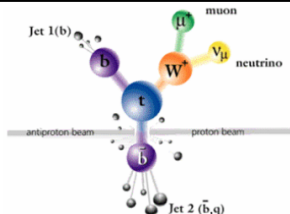


# CDF ME inputs (B. Stelzer)

- Input to the Matrix Element Analysis are the measured four-vectors of the Lepton, Jet1 and Jet2 in the W+2jets data ( $\geq 1$  b-tagged jet)



# Matrix element method - Probability (B. Stelzer)



Event probability for signal and background hypothesis:

$$P(p_i^\mu, p_{j1}^\mu, p_{j2}^\mu) = \frac{1}{\sigma} \int d\rho_{j1} d\rho_{j2} d\rho_\nu^z \sum_{comb} |M(p_i^\mu)|^2 \frac{f(q_1)f(q_2)}{|q_1||q_2|} \phi_4 W_{jet}(E_{jet}, E_{part})$$

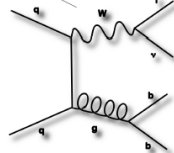
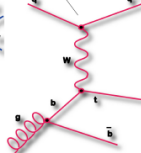
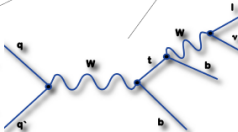
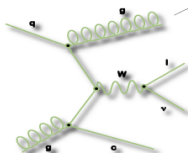
Input only lepton and 2 jets 4-vectors!

Integration over part of the phase space  $\Phi_4$

Leading Order matrix element (MadEvent)

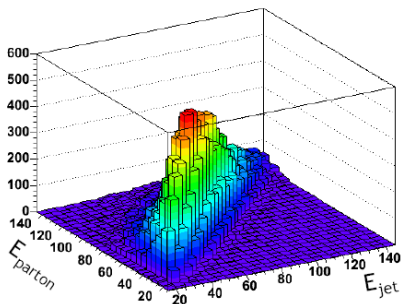
$W(E_{jet}, E_{part})$  is the probability of measuring a jet energy  $E_{jet}$  when  $E_{part}$  was produced

Parton distribution function (CTEQ5)

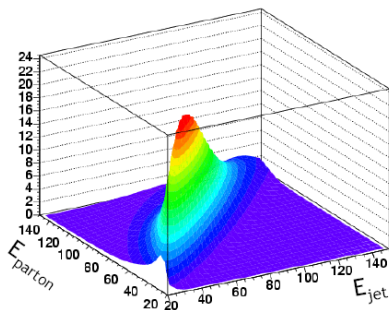


# Matrix element method - CDF transfer functions

Full simulation vs parton energy:



Double Gaussian parameterization:



Double Gaussian parameterization:

$$W_{jet}(E_{jet}, E_{parton}) = \frac{1}{\sqrt{2\pi}(p_1 + p_2 p_5)} \left[ \exp \frac{-(\delta_E - p_1)^2}{2p_2^2} + p_3 \exp \frac{-(\delta_E - p_4)^2}{2p_5^2} \right]$$

$$\text{where: } p_i = a_i + b_i E_{parton} \quad \delta E = (E_{parton} - E_{jet})$$



# Matrix element method - DØ transfer functions

- ◆ To evaluate  $|M|^2$ , we must have initial/final state 4-vectors.

- ◆  $W(x,y)$  relates final state  $y$  to detector state  $x$

- ◆ Jets

- ◆ Assume angles well measured and Sole dependence on energy difference

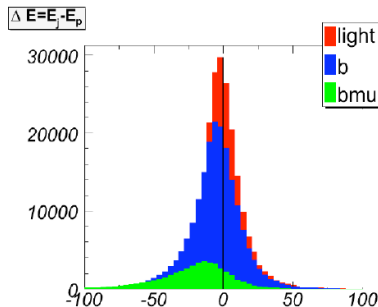
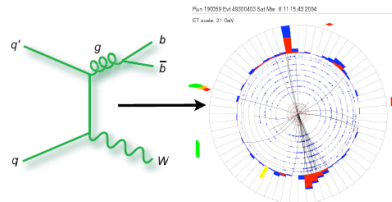
- ◆ Calculate for 3 types of jets: light, b, and b w/ mu

- ◆ Electrons

- ◆ Assume angles well measured and sole dependence on energy difference

- ◆ Muons

- ◆ Dependence on  $q/P_T$ ,  $\eta$ , and number of SMT hits



# W+jets heavy flavour fraction at DØ

$$\alpha(Wb\bar{b} + Wc\bar{c}) + Wjj + t\bar{t} + \text{QCD} = \text{Data}$$

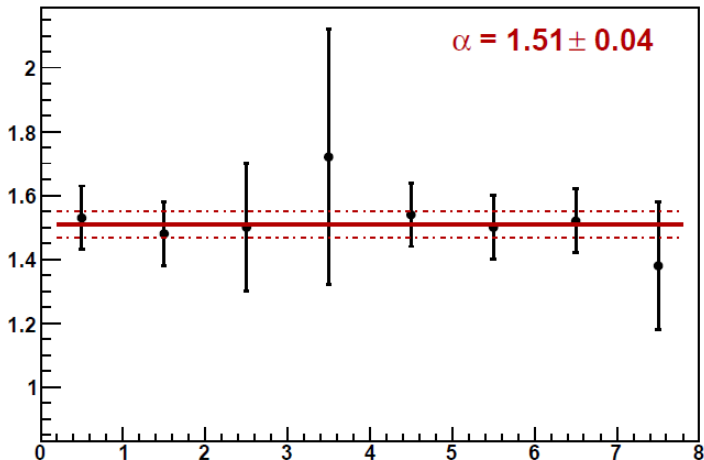
Scale Factor  $\alpha$  to Match Heavy Flavor Fraction to Data

	1 jet	2 jets	3 jets	4 jets
Electron Channel				
0 tags	$1.53 \pm 0.10$	$1.48 \pm 0.10$	$1.50 \pm 0.20$	$1.72 \pm 0.40$
1 tag	$1.29 \pm 0.10$	$1.58 \pm 0.10$	$1.40 \pm 0.20$	$0.69 \pm 0.60$
2 tags	—	$1.71 \pm 0.40$	$2.92 \pm 1.20$	$-2.91 \pm 3.50$
Muon Channel				
0 tags	$1.54 \pm 0.10$	$1.50 \pm 0.10$	$1.52 \pm 0.10$	$1.38 \pm 0.20$
1 tag	$1.11 \pm 0.10$	$1.52 \pm 0.10$	$1.32 \pm 0.20$	$1.86 \pm 0.50$
2 tags	—	$1.40 \pm 0.40$	$2.46 \pm 0.90$	$3.78 \pm 2.80$



# HF Fraction - $D\bar{D}$

Heavy flavour scale factor  $\alpha$  measured in the zero tag bins



# HF Fraction - CDF (B. Stelzer)

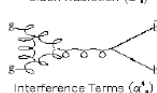
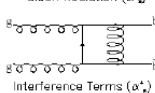
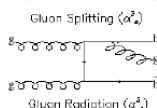
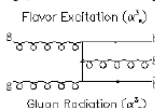
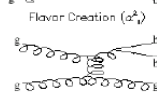
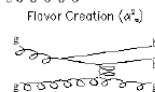
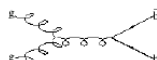
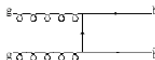
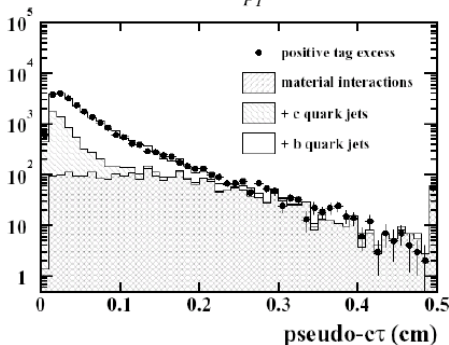
- 1) Estimate generic jet heavy flavor fraction in ALPGEN Monte Carlo
- 2) Fit for bottom and charm fraction in generic jet data

Difference between the two outcomes suggests  $K=1.5 \pm 0.4$

Result supported by study using MCFM:

J. M. Campbell, J. Houston,  
Method 2 at NLO, hep-ph/0405276

$$pseudo-c\tau = L_{2D} \cdot \frac{M^{vx}}{p_T^{vx}}$$





# Binned likelihood fit at CDF (B. Stelzer)

## Binned Likelihood Function:

$$\mathcal{L}(\beta_1, \dots, \beta_5; \delta_1, \dots, \delta_{10}) = \underbrace{\prod_{k=1}^B \frac{e^{-\mu_k} \cdot \mu_k^{n_k}}{n_k!}}_{\text{Poisson term}} \cdot \underbrace{\prod_{j=2}^5 G(\beta_j | 1, \Delta_j)}_{\text{Gauss constraints}} \cdot \underbrace{\prod_{i=1}^{10} G(\delta_i, 0, 1)}_{\text{Systematics}}$$

## Expected mean in bin k:

$$\mu_k = \sum_{j=1}^5 \beta_j \cdot \underbrace{\left\{ \prod_{i=1}^{10} [1 + |\delta_i| \cdot (\epsilon_{ji+} H(\delta_i) + \epsilon_{ji-} H(-\delta_i))] \right\}}_{\text{Normalization Uncertainty}}$$

$$\underbrace{\cdot \alpha_{jk}}_{\text{Shape } P.} \cdot \underbrace{\left\{ \prod_{i=1}^{10} (1 + |\delta_i| \cdot (\kappa_{jik+} H(\delta_i) + \kappa_{jik-} H(-\delta_i))) \right\}}_{\text{Shape Uncertainty}}$$

$\beta_j = \sigma_j / \sigma_{SM}$  parameter  
 single top (j=1)  
 W+bottom (j=2)  
 W+charm (j=3)  
 Mistags (j=4)  
 ttbar (j=5)  
 k = Bin index  
 i = Systematic effect  
 $\delta_i$  = Strength of effect  
 $\epsilon_{ji\pm} = \pm 1\sigma$  norm. shifts  
 $\kappa_{jik\pm} = \pm 1\sigma$  shift in bin k

- All sources of systematic uncertainty included as nuisance parameters
- Correlation between Shape/Normalization uncertainty considered ( $\delta_i$ )

# Measuring cross sections at $D\bar{O}$

Probability to observe data distribution  $D$ ,  
expecting  $y$ :

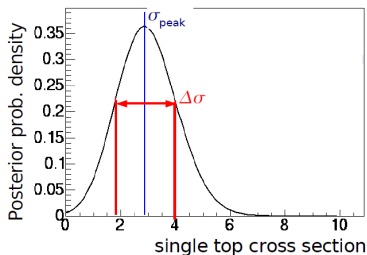
$$y = \alpha/\sigma + \sum_{s=1}^N b_s \equiv a\sigma + \sum_{s=1}^N b_s$$

$$P(D|y) \equiv P(D|\sigma, a, b) = \prod_{i=1}^{nbins} P(D_i|y_i)$$

The cross section is obtained

$$Post(\sigma|D) \equiv P(\sigma|D) \propto \int_a \int_b P(D|\sigma, a, b) Prior(\sigma) Prior(a, b)$$

- Bayesian posterior probability density
- Shape and normalization systematics treated as nuisance parameters
- Correlations between uncertainties properly accounted for
- Flat prior in signal cross section



- No assumptions on the number of families or unitarity of the CKM matrix
- However, some other model assumptions have been made
- It is assumed that the only existing production mechanism of single top quarks involves the interaction with a  $W$  boson (models where single top quark events can be produced e.g. via FCNC interactions or heavy scalar or vector boson exchange, are not considered)
- Assuming  $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$ , implying  $B(t \rightarrow Wb) \simeq 100\%$
- Finally,  $tbW$  interaction is CP-conserving and of the  $V-A$  type, but it is allowed to have an anomalous strength
- Most general  $tbW$  vertex:

$$\Gamma_{tbW}^\mu = -\frac{g}{\sqrt{2}} V_{tb} \bar{u}(p_b) \left[ \gamma^\mu (f_1^L P_L + f_1^R P_R) - \frac{i\sigma^{\mu\nu}}{M_W} (f_2^L P_L + f_2^R P_R) \right] u(p_t)$$

- SM: CP is conserved in the  $tbW$  vertex,  $f_1^L = 1$  and  $f_1^R = f_2^L = f_2^R = 0$

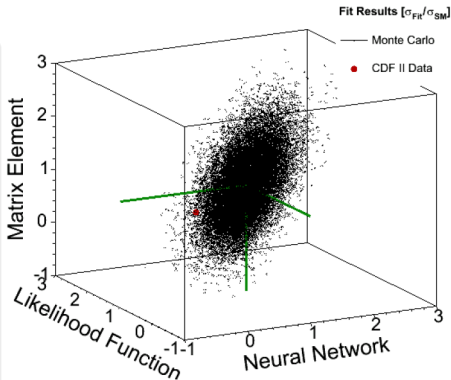


# CDF compatibility study

- ME, NN and LF analyses use same input dataset and MC events, but results differ

## Potential sources of differences

- ME uses transfer functions
- ME does not use missing ET
- ME integrates over all neutrino  $p_z$ , while NN chooses the solution with smaller  $|p_z|$
- with two jets in the event, the NN choose the secondary-vertex-tagged jet as the  $b$  jet from top quark decay. The ME sums over both possibilities
- NN also allows for soft jets ( $8 < E_T(jet) < 15$  GeV)

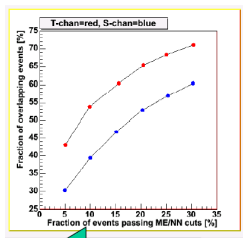


- LF(t), ME(s+t), NN(s+t)
- Coming: all six discriminants: LF(s), LF(t), ME(s+t), NN(s), NN(t), NN(s+t)

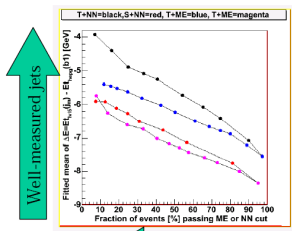


# CDF compatibility study (cont'd)

- Overlap between 5% highest-ME and 5% highest-NN(s+t) events is 30(43)% for s(t)-channel (left plot)
- Impact of transfer functions (middle plot): NN needs better-measured jets in signal region (close to 0) than ME. Significant effect in t-channel only (black/blue curves)
- Missing ET measurement (right plot): NN needs better-measured MET in signal region (close to 0) than ME

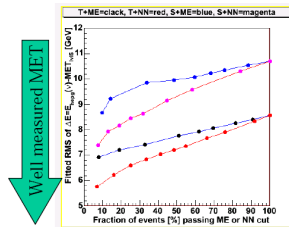


Signal-likeness



Well-measured jets

Signal-likeness



Well measured MET

Signal-likeness

